C1WS4K
Introduction: Convention of Expressing Any Base 10 Number As a Product of a Number Between One and 9 , multiplied by 10 to the Power of Some Exponent.

Exponentiation is the replication of multiplication the way multiplication is the replication of addition
$10^{0}=1$
$10^{1}=10$
$10^{-1}=1 / 10=0.1$
$10^{2}=10(10)=100$
$10^{-2}=1 /[10(10)]=1 / 100=0.01$
$10^{3}=10(10)(10)=1000$
$10^{-3}=1 /[101(10)(10)]=1 / 1000=0.001$

## Advantages of Scientific Notation:

1. Allows Awkwardly Large and Small Numbers to Be Expressed in Term of Compact and Easily Written Numbers
2. Allows Accurate Representation of the Number of Significant Figures in a Number, That Is a Measurement's Precision, the "Certainty" of Our Measurements

## Convert the following numbers to scientific notation

0.00456 and 456.00

## A) $\mathbf{0 . 0 0 4 5 6}$ (A number smaller than 1)

Step 1: Since this number is less than 1 you need identify the power of 10 which you can multiply it by and set one digit to the left of the decimal. Here, we can multiply by 1000 or $10^{3}$ and force the original number to have one digit to the left of the decimal, but we have changed its value.
$0.00456 \times 10^{3}=4.56$ (note, which is not equal to the original number)
Step 2: Since we multiplied it by $10^{3}$ we must also divide by $10^{3}$ (effectively multiplying the original number by 1 and not changing it's value). Than we express the factor in the denominator as a power of 10 .
0.00456
$=0.00456 x \frac{10^{3}}{10^{3}}$
$=\frac{0.00456 \times 10^{3}}{10^{3}}$
$=\frac{4.56}{10^{3}}$
$=4.56 \times 10^{-3}$

Note, once you get the hang of this you can just count the number of digits you need to move the decimal to bring the original number to one digit to the left of the decimal and multiply that number by 10 to the negative value of those digits. Here we moved the decimal three positions to the right, so we multiply by $10^{-3}$ (ie., divide by $10^{3}$ ).

## B. 456.00, (A number larger than 10)

Since this number has a value greater than 9 we must divide it by a factor of 10 to make the first non-zero digit value between 1 and 9 .
456.00
$=456.00 \frac{10^{2}}{10^{2}}$
$=\frac{456.00}{10^{2}} \times 10^{2}$
$=4.56 \times 10^{2}$
Note, once you get the hang of this you can just count the number of places you move the decimal to the right (resulting in a value with one digit to the left of the decimal) and then multiply by 10 to the power of that number ( 2 in this case).

## Using Scientific Notation to Express Significant Digits:

How can you express the number 400 to 2 significant digits?
You must use scientific notation.
$4.0 \times 10^{2}$
As scientific notation always has a decimal point there is never a problem expressing significant digits.

## Problem Set 1:

Convert the following measured values to scientific notation and express answers to the proper number of significant figures.
a. $0.00045602=4.5602 \times 10^{-4}$
b. $50444000=5.0444 \times 10^{7}$
c. $50444000 .=5.0444000 \times 10^{7}$
d. $32.010=3.2010 \times 10$
e. $253=2.53 \times 10^{2}$
f. $0.0034=3.4 \times 10^{-3}$

## Multiplication of numbers in Scientific notation

Try plugging the following number into your calculator. Odds are you will get an error message.
$\frac{\left(9.47 \times 10^{598}\right)\left(7.39 \times 10^{-98}\right)}{\left(1.432 \times 10^{-645}\right)\left(2.46 \times 10^{4}\right)}$
You will often get numbers which are bigger or smaller than a calculator can handle. You need to treat the power separately from the number, so break into two terms.

$$
\begin{aligned}
& \frac{\left(9.47 \times 10^{598}\right)\left(7.39 \times 10^{-98}\right)}{\left(1.432 \times 10^{-645}\right)\left(2.46 \times 10^{4}\right)} \\
& =\left(\frac{9.47 \times 7.39}{1.432 \times 2.46}\right)\left(\frac{10^{598} \times 10^{-98}}{10^{-645} \times 10^{4}}\right)= \\
& =19.866 \times 10^{(598-98+645-4)} \\
& =19.9 \times 10^{1141}=1.99 \times 10^{1142}
\end{aligned}
$$

## Addition and Subtraction of Numbers in Scientific Notation

Consider the following problem
$4.860 \times 10^{12}+9.7 \times 10^{10}+3.68 \times 10^{11}$
You first need to express all numbers to the same power so you can line up the decimal point. It is suggested that you choose the largest power and make everything else a fraction.

$$
\begin{array}{r}
4.860 \times 10^{12} \\
+0.097 \times 10^{12} \\
+0.368 \times 10^{12} \\
\hline 5.325 \times 10^{12}
\end{array}
$$

## Scientific Notation Key

## C1WS4K

Problem Set 2: Solve the following problems

1. $3.03860 \times 10^{-32}+3.7 \times 10^{-30}+3.68 \times 10^{-31}$

$$
\begin{aligned}
& 3.7 \times 10^{-30} \\
+ & 0.368 \times 10^{-30} \\
+ & 0.03860 \times 10^{-30} \\
\hline & 4.1066 \times 10^{-30}=4.1 \times 10^{-30}
\end{aligned}
$$

2. $3.03860 \times 10^{-32}-3.7 \times 10^{-30}+3.68 \times 10^{-31}$

$$
\begin{aligned}
& -3.7 \times 10^{-30} \\
& +0.368 \times 10^{-30} \\
& +0.03860 \times 10^{-30} \\
& -3.2934 \times 10^{-30}=-3.3 \times 10^{-30}
\end{aligned}
$$

3. $\frac{\left(9.7 \times 10^{583}\right)\left(7.339 \times 10^{98}\right)}{\left(5.432 \times 10^{-645}\right)\left(3.446 \times 10^{-4484}\right)}=\left(\frac{9.7 \times 7.339}{5.432 \times 3.446}\right) \times 10^{(583+98+645+4484)}=3.8 \times 10^{5810}$
4. $\frac{\left(9.7 \times 10^{583}\right)\left(7.339 \times 10^{-98}\right)}{\left(5.432 \times 10^{-645}\right)\left(3.446 \times 10^{484}\right)}=\left(\frac{9.7 \times 7.339}{5.432 \times 3.446}\right) \times 10^{(583-98+645-4884)}=3.8 \times 10^{-3354}$
5. $\frac{\left(9.700 \times 10^{583}\right)\left(7.339 \times 10^{98}\right)}{\left(5.432 \times 10^{-645}\right)\left(3.446 \times 10^{-4484}\right)}=\left(\frac{9.700 \times 7.339}{5.432 \times 3.446}\right) \times 10^{(583+98+645+4484)}=3.803 \times 10^{5810}$
6. $\frac{\left(9.70 \times 10^{-583}\right)\left(7.339 \times 10^{-98}\right)}{\left(5.432 \times 10^{645}\right)\left(3.446 \times 10^{4484}\right)}=\left(\frac{9.70 \times 7.339}{5.432 \times 3.446}\right) \times 10^{(-583-98-645-4484)}=3.80 \times 10^{-5810}$
7. 

$$
\frac{\left(9.70 \times 10^{5}+6.3 \times 10^{4}\right)\left(3.33 \times 10^{5}\right)}{\left(5.00 \times 10^{45}\right)\left(3.20 \times 10^{-5}\right)}=\frac{\left(1.033 \times 10^{6}\right)\left(3.33 \times 10^{5}\right)}{\left(5.00 \times 10^{45}\right)\left(3.20 \times 10^{-5}\right)}
$$

$$
=\left(\frac{1.033 \times 3.33}{5.00 \times 3.20}\right) \times 10^{(6+5-45+5)}=0.21499 \times 10^{-29}=2.15 \times 10^{-30}
$$

